

# PDP: Prolog Distributed Processor for Independent AND\OR Parallel Execution of Prolog <sup>1</sup>

Lourdes Araujo  
Jose J. Ruz  
Dpto.Informática y Automática  
Universidad Complutense de Madrid  
Madrid 28040, Spain  
{lurdes, jjruz}@dia.ucm.es

## Abstract

PDP (Prolog Distributed Processor) is a multisequential system for Independent AND\OR parallel execution of Prolog. The system is composed of a set of workers controlled hierarchically. Each worker operates on its own private memory and interprocessor communication is performed only by the passing of messages. Independent AND\_parallelism is exploited following a *fork-join* scheme and OR\_parallelism is exploited following a multisequential approach. Both kinds of parallelism are implemented using closed environments. To exploit OR\_parallelism, the parent worker environment is reconstructed in a new worker by *recomputing* the initial goal without backtracking, following the *success path* obtained from the parent worker. PDP deals with OR\_under\_AND parallelism producing the solutions of a set of parallel goals in a distributed way, that is, creating a new task for each element of the cross product. This approach has the advantage of avoiding both storing partial solutions and synchronizing workers, resulting in a largely increased performance. PDP has been implemented on a transputer network and performance results show that PDP introduces very little overhead into sequential programs, and provides a high speedup for coarse grain parallel programs.

## 1 Introduction

There are a considerable number of approaches proposed for the parallel execution of Prolog, dealing with OR\_parallelism [1, 4, 5, 2], Independent AND\_parallelism [10, 12, 14, 7], and recently combining AND-OR parallelism [19, 3, 11]. Since most of these approaches are implemented on systems with totally or partially shared memory, we are interested in investigating the possibilities of a completely distributed model of processing, that eliminates the shared memory contention.

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In this paper we present the Prolog Distributed Processor, a multisequential system supporting both Independent AND and OR\_parallelism. In order to reduce the communications overhead, PDP has been designed with a hierarchic control. PDP is composed of a set of clusters, each of them consisting of a *controller* and a set of *workers*. Controllers are responsible for the distribution of pending work among idle workers. When every worker in a cluster is busy, the work may be sent to other clusters. Each worker operates on its own private memory and interprocessor communication is performed only by the passing of messages. In order to reduce communication overhead, each worker follows a *closed environment approach* [6], that is, there are no variables in a worker defined in terms of variables that belong to other worker.

The goals and clauses to be executed in parallel (*parallel goals* and *parallel clauses*) are supposed to be annotated in the program, either by the compiler [7, 15] in AND\_parallelism or by the user in OR\_parallelism. The execution model has been developed as an extension of the Warren Abstract Machine (WAM) [18], maintaining both the optimization of the sequential Prolog techniques and the speedup of the Independent AND\_parallel system and the multisequential OR\_parallel system.

In the case of AND\_parallelism, parallel goals are sent along with their variable bindings, to the idle worker indicated by the controller and an answer is then awaited by the parent worker. In order to control the execution of a parallel call, we have modified the shared memory model developed by Hermenegildo [12] for a distributed system.

The exploitation of OR\_parallelism is based on the multisequential execution of the branches of the search tree, splitting the work dynamically. When a worker finds a parallel clause, it makes the new work available for idle workers, by sending a warning to the controller. Since each processor works in its own environment, the parent worker environment has to be reconstructed by the worker which assumes the new work. Instead of copying the environment as MUSE [1], PDP *recomputes* [2] the initial goal without backtracking, following the *success path* obtained from the parent worker (Figure 1). The amount of data communicated with this approach is smaller than that of the copying approach, which in turn speeds up the execution on a distributed system.

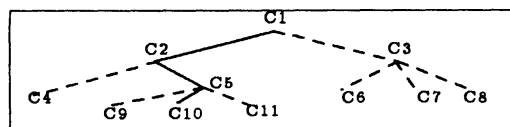


Figure 1: Recomputation following the success path C2,C5,C10

For programs presenting OR\_under\_AND parallelism the different solutions of each goal in a *parallel call* (set of parallel goals) have to be combined.

In the AND\_parallelism approach the task carrying out a parallel goal reaches the successive solutions sequentially, when they are required because of backtracking. Therefore, if there is OR\_parallelism in a parallel goal, maintaining the AND\_parallelism approach requires the storing of the different solutions until required for building a new combination. The PDP approach avoids storing partial solutions and synchronizing workers. The idea is to create a new computation for each combination of solutions, recomputing the success path from the initial goal of the program until the parallel call is reached. In this way, the exploitation approach of AND\_parallelism becomes that of OR\_parallelism, which creates independent computations. This avoids the communications overhead of the AND\_parallelism approach which is due to both the sending of solutions to the parent task and the requirements of new solutions from the offspring tasks. This is the reason why the speedup achieved by exploiting both kinds of parallelism may be greater than the product of the speedup achieved by exploiting each kind of parallelism separately. To avoid repeating solutions, we have introduced a *combination rule* to set the combinations corresponding to each new task.

The rest of the paper proceeds as follows: section 2 presents the execution model. Section 3 describes the parallel tasks of PDP. Section 4 presents a PDP execution scheme. Section 5 describes the scheduling policy. Results are presented in section 6 and finally conclusions drawn in section 7.

## 2 Execution Model

PDP exploits pure AND\_parallelism, pure OR\_parallelism and the combination of both, producing *OR\_tasks* which explore the search tree branches from the root, and *AND\_tasks* which execute parallel goals. The PDP approach to exploit combined parallelism – when it appears in the form OR\_under\_AND – is based upon the fact that the recomputation allows the AND\_tasks to exploit OR\_parallelism by creating OR\_tasks. Therefore in the combined model both kinds of parallelism are joined in a very natural way. Another important point is that the search tree is automatically distributed among the workers by means of a distribution rule, so that no worker is in charge of the distribution. The model is outlined as follows:

- The execution of a program begins as an OR\_task, that records the success path.
- If AND or OR\_parallelism appear, new AND or OR\_tasks are created, respectively.
- If an AND\_task finds OR\_parallelism, it creates a new OR\_task to deal with the parallel clauses and transfers to it the success path leading to the parallel call. Notice that the AND\_task at this point has received this information for this purpose only. In this way, the

exploitation approach of AND\_parallelism becomes that of OR\_parallelism, and this reduces the exchange of information.

- Once the recomputation of this OR\_task arrives to the parallel call from where it originates, if the operation were to blindly exploit the OR\_parallelism, the result would be the simple repetition of solutions. In order to avoid this we have introduced a *combination rule* which decides the branch to be explored to solve each parallel goal. Let us call any goal which presents OR\_parallelism and causes the creation of OR\_tasks, the ancestor goal of these tasks. The key point of this rule is to fix the solution of the goals on the left of the ancestor goal and to combine them with every solution of the remaining goals. The *combination rule* is as follows:

- If the goal is on the left of the ancestor goal, the branch to be explored is *fixed* to that explored by the previous “forefather” OR\_task.
- If the goal is the ancestor goal, the branch to be explored is the next one to that explored by the AND\_task.
- If the goal is on the right of the ancestor goal, the branch to be explored is the one leading to the first solution.

A new structure is introduced to specify the untried clauses: the *cross product environment* (CPE), associated to each parallel call. It is composed of a pointer marking the beginning of the success path corresponding to each goal in a parallel call.

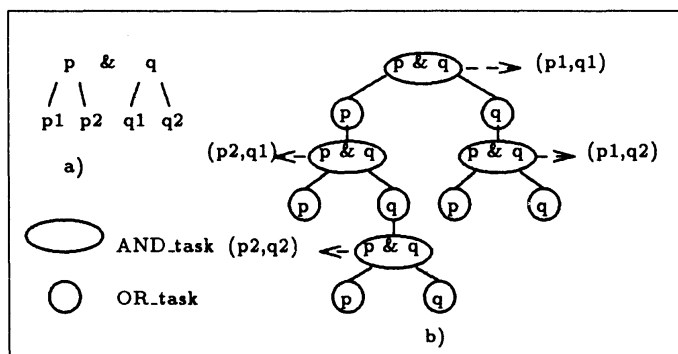


Figure 2: OR\_under\_AND parallelism in PDP

In order to visualize this process consider the program represented in Figure 2a), whose execution is shown in Figure 2b). When the AND\_tasks which execute the parallel goals  $p$  and  $q$  find OR\_parallelism, the first alternative clauses  $p1$  and  $q1$  are explored to give the answer to the parent task, and new OR\_tasks are created to explore  $p2$  and  $q2$ . For the OR\_task

corresponding to  $(p2, q1)$   $p$  is the ancestor goal and therefore, the branch to be explored so as to solve  $p$  corresponds to  $p2$  ( $p1$  is already being explored by the parent AND\_task). Since  $q$  is on the right of the ancestor goal, the branch to be explored is  $q1$ , the first one. For the OR\_task corresponding to  $(p2, q2)$  the ancestor goal is  $q$  and therefore, the branch to be explored to solve  $p$  (which is on the left) is  $p2$ , the same as that explored by the previous forefather OR\_task, i.e. that corresponding to  $(p2, q1)$ . For  $q$  the branch to be explored is  $q2$ , the following branch to the one explored by the parent AND\_task.

### 3 Parallel Tasks in PDP

The PDP approach to exploit OR\_under\_AND parallelism leads to the distinction between different kinds of OR and AND\_tasks depending both on the kind of task it arose from and on the ancestor goal position. The kinds of tasks are:

- **Primary OR\_task:**  
This arises from the OR\_parallelism exploitation in an OR\_task. When the recomputation of the received success path is completed, the execution follows in the normal way.
- **Secondary OR\_task:**  
This arises from the OR\_parallelism exploitation in an AND\_task. When the recomputation of the success path leading to the parallel call is finished, a new combination of solutions is created.
- **Primary AND\_task:**  
This arises from the AND\_parallelism exploitation in an AND\_task, a primary OR\_task or a secondary OR\_task provided the latter does not correspond to a goal on the left of the ancestor goal. Primary AND\_tasks exploit OR\_parallelism appearing during the execution.
- **Secondary AND\_task:**  
This arises from the AND\_parallelism exploitation in a secondary OR\_task corresponding to a goal on the left of the ancestor goal. According to the combination rule, this task must ignore any OR\_parallelism appearing during the execution.

Producer and consumer relationships of the tasks can be shown pictorially as a *task tree*. In general, the task tree and the search tree are different, since it is not always possible, neither suitable to exploit all the potential parallelism of the program. Figure 3 shows a PDP execution example corresponding to the following program.

```
:- p & q.
p :- p1.      q :- q1.
p :- p2.      q :- q2.
p :- p3.
```

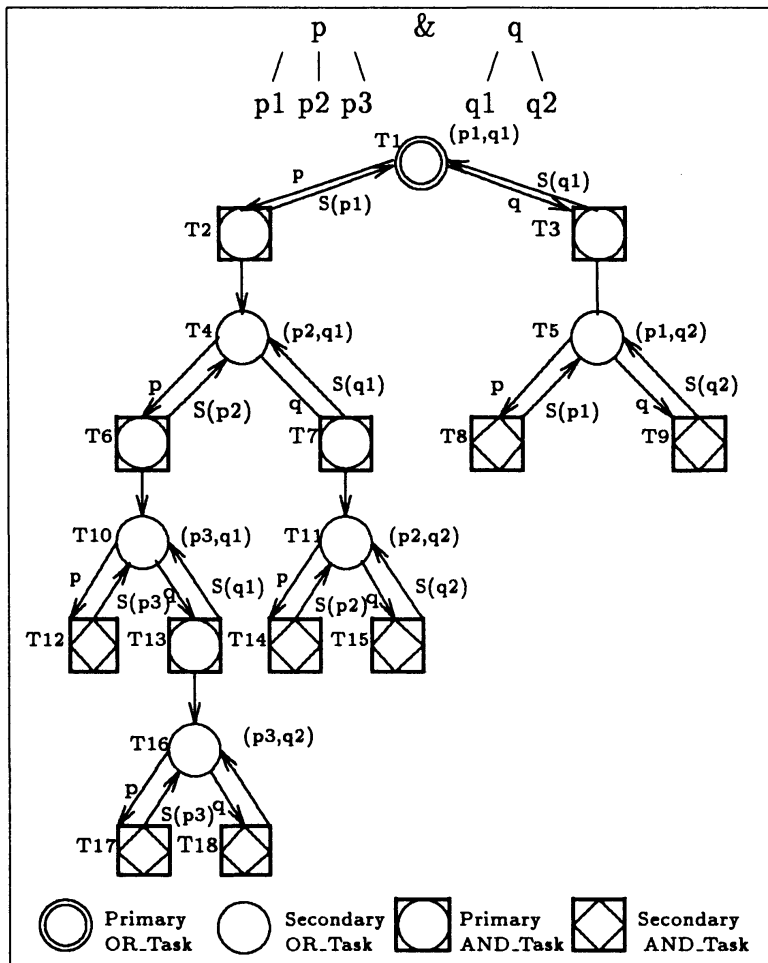


Figure 3: PDP execution example

The first solution of the parallel call  $p \& q$  is obtained with the clauses  $p_1$  and  $q_1$  of  $p$  and  $q$  respectively. If a failure occurs or new solutions are required, there is a number of pending alternatives to obtain the solutions, corresponding to the cross product of  $p$  and  $q$ :  $(p_1, q_2)$ ,  $(p_1, q_3)$ ,  $(p_2, q_1)$ , etc. The execution begins as a primary OR\_task that finds a parallel call and creates the AND\_tasks T2 and T3. When the goal  $p$  is executed, T2 finds OR\_parallelism, then it takes the first clause  $p_1$ , explores it by itself and creates a new secondary OR\_task, T4, for exploring a new solution. T1 builds the CPE  $(p_1, q_1)$ , that is passed to T2 and T3. T2 builds the CPE  $(p_1, q_1)$  because the ancestor goal (\*) is the first one. The next combination corresponding to this CPE is passed to T4 which takes the next clause,  $p_2$ , for the goal marked as the ancestor one, and the first one for every goal on the right,  $q_1$ . T5 receives  $(p_1, q_2)$ , indicating that the alternative clause to exploit for  $p$  is the first one and for  $q$  it is the second one.

```

type res_type = (success, fail);
type task_type = (primary_AND, secondary_AND, primary_OR, secondary_OR);
process AND_task( $\rho$ :program; Q:goal; V:substitution;
                 C:success path; CPE: cross product env.; tasktype: task_type);
var
  R: resolvent; result: res_type; S: backtracking stack;
begin
  R := [Q]; S :=  $\emptyset$ ; C := C[CPE[Q]];
  recomputation( $\rho$ , R, S, V, C, CPE);
  if R  $\neq \emptyset$  then
    execution( $\rho$ ,R,S,V,C,CPE,tasktype,result); end
  else result := success; end
  if result = success then send_success(parent_task, restriction(V,Q), alternative);
  else send_fail(parent_task);
end

```

Figure 4: AND\_task creation

The scheme of creation of an AND\_task is shown in Figure 4. The entry to an AND\_task consists of a goal along with its variable bindings  $V$ , the success path  $C$  and the CPE corresponding to the received goal. The program and the kind of AND\_task to be created are also received. The *resolvent*  $R$  and the *backtracking stack*  $S$  (where the state is saved) are initialized. The new AND\_task takes from the received success path  $C$  the part which corresponds to the goal to be executed, starting at the point indicated in the CPE. The success path of the goal may be empty, incomplete or complete, depending on both the kind of task and on the position of the goal in the parallel call. If after the recomputation of the success path of the goal the resolvent is not empty, the pending execution is performed. The answer obtained is sent to the parent task.

```

process OR_task( $\rho$ :program;Q:goal; C:success path;
                CPE: cross product env.; tasktype: task_type)
var
  S : backtracking stack; V: substitution; R: resolvent;
begin
  R := [Q]; S :=  $\emptyset$ ;
  recomputation( $\rho$ ,R,S,V,C,CPE);
  execution( $\rho$ ,R,S,V,C,CPE,tasktype,result);
  if result = success then
    V := restriction(V,Q);
    display(V,result);
end

```

Figure 5: OR\_task creation

The scheme of creation of an `OR_task` is shown in Figure 5. An `OR_task` receives as entry the success path and the CPE of the parent task. The program along with the goal to be executed and the kind of `OR_task` to be created are also received. After initializing the resolvent and the backtracking stack, the recomputation of the success path is performed. This recomputation produces an environment consisting of a resolvent, a backtracking stack and a substitution. Then, the execution of the pending resolvent is performed. Once it is finished the result is presented to the user.

## 4 PDP Execution Scheme

Figure 6 shows the PDP execution scheme. Following the resolution algorithm, the resolvent is transformed until it becomes empty (successful execution) or a failure occurs. In each resolution step, a set of independent goals is taken from the resolvent (`AND_parallelism`). Each independent goal is solved by a different `AND_task` except the first one which is executed by the parent task itself. If the created `AND_task` is *primary*, the CPE is updated to a new combination, and the answers corresponding to goals executed by other tasks are awaited (`waited_answer = 0`). For the goals whose computation succeeds, the computed answer substitution obtained is received and composed with the computed answer substitution of the current task. If all computations succeed, the resolution process continues. The resolution of an only goal ( $r = 1$ ) *unifies* the goal with the head of a clause of the associated predicate. If there is `OR_parallelism`, `OR_tasks` are created to perform the unification of the goal with other clauses, removing these pending alternative clauses in the parent processor. If the created `OR_task` is *secondary* the CPE is updated to a new combination. If the execution of the goal succeeds, the state is *saved* in the backtracking stack, the substitution obtained and the previous one are *composed*, the goal is *replaced* by the body of the clause in the resolvent, and the alternative clause considered is recorded in the *success path*. If the execution fails, backtracking will be performed taking a previous state out the backtracking stack.

## 5 Scheduling Policy

The controllers are responsible for the distribution of pending work among idle workers. At initialization time, each worker is loaded with the same program and the execution starts in one of them. A worker will be in one of the three states: *idle* (without work), *busy* (working) or *offering* (with pending work). The controller is warned about idle and offering workers informing to the idle workers which offering worker has to be requested for work. To optimize the communications, the workers do not report every change in



```

procedure execution( $\rho$ :program; R:resolvent; S:backtracking stack; V:substitution
  C: success path; CPE: cross product env.; tasktype:task_type; result:res_type);
var
  a: goal;  $P_a$ : associated procedure to goal a;
  c: clause;  $V'$ : substitution; r: integer;
begin
  repeat
     $[A_1, \dots, A_r] := \text{independent\_set}(R)$ ;  $r = \text{size}([A_1, \dots, A_r])$ ;
    if  $r > 1$  then begin
      waited_answers := 0;
      for  $i := 2$  to  $r$  /* AND PARALLELISM */
        if tasktype = primary_OR_task or
          tasktype = primary_AND_task or
          tasktype = secondary_OR_task and ancestor_goal(CPE)  $\leq i$  then
          AND_task( $\rho, A_i, \text{restriction}(V, (A_i)), C, \text{new\_comb}(CPE), \text{primary}$ );
        else
          AND_task( $\rho, A_i, \text{restriction}(V, (A_i)), C, CPE, \text{secondary}$ );
          waited_answers := waited_answers + 1; end
      execution( $\rho, [A_1], S, V, C, CPE, \text{tasktype}, \text{result}$ );
      while waited_answers  $> 0$  and result = success do begin
        result := receive_answer( $i, \theta_i$ );
        waited_answers := waited_answers - 1;
        if result = success then begin
          R := apply( $\theta_i, R$ );
          V := V  $\circ \theta_i$ ; end
      end
    end
  else begin /*  $r = 1$  */
    a := R[1] /* The first atom in the resolvent is taken */
    search_procedure(a,  $\rho, P_a$ ); /* associated procedure to the goal a */
    repeat
      c :=  $P_a[1]$ ; /* The first pending clause in the procedure is taken */
       $P_a := P_a - c$ ;
      if OR_parallelism(c) then
        if tasktype = AND_task or tasktype = secondary_OR_task then
          OR_task( $\rho, R, V, C, \text{new\_comb}(CPE), \text{secondary}$ );
        else
          OR_task( $\rho, R, V, C, CPE, \text{primary}$ );
           $P_a := P_a - P_a[1]$ ; end
      result := unify(a, c,  $V'$ );
      until ( $P_a = []$ ) or result = success;
      if result = success then begin
        if  $P_a \neq []$  then save( $P_a, R, V, S$ );
        V := compose(V,  $V'$ );
        replace(R, a, c); /* In R, replace a by c body */
        push(c, C); end /* The explored alternative is write in C */
      end
    if result = fail then backtracking( $\rho, S, R, V, C, \text{result}$ );
  until (R = []) or result = fail;
end

```

Figure 6: PDP execution scheme

program	strategy A	strategy B	strategy C
query	3.4	3.2	3.3
zebra	3.9	3.5	3.6
mm	4.5	4.3	4.3
queen(8)	12.9	11.9	12.6
queen(9)	14.2	13.5	13.8
queen(10)	14.7	14.5	14.5

Table 1: Speed-up for different scheduling policies

their work load. The controller has exact information about idle workers and offering workers, and approximate information about the workers load.

In order to choose the offering worker which is going to share work with an idle worker, several strategies previously used by different systems [16, 13] have been tested.

- strategy A: Choose the nearest (physical distance) idle worker to the offering worker
- strategy B: Choose the most loaded offering worker
- strategy C: Choose the oldest offer

Table 1 shows the speedup on a system with 15 workers for each strategy. Since the measured times differ from run to run, all speedups given are computed using the average times of three runs. The example programs examined are standard benchmarks for AND\_parallel systems, the *queen* problem, *query*, a database problem, *zebra*, a puzzle and *mm*, the mastermind program. The results show that the best strategy is A, choosing the nearest idle worker to the offering worker. This strategy optimizes the traffic in the network and favours exchanges between workers which have shared work previously, optimizing OR\_parallelism exploitation. The worst strategy is B, since it is the most expensive one (it requires more information exchange than the other), while strategy C, choosing the oldest request is almost as good as A, since it is the cheapest one in that it doesn't need any analysis by the controller.

Because of the overhead associated with the parallel execution, the *granularity* of a job, i.e. an estimate of the amount of work needed to solve it, should be taken into account [8, 9, 17] when deciding whether or not to execute a job as a separate task. PDP applies control mechanisms based on heuristic observations about memory occupation.

Measurements have shown the similarity of the amount of data in the stack when each solution is reached. Therefore, it is possible to estimate how

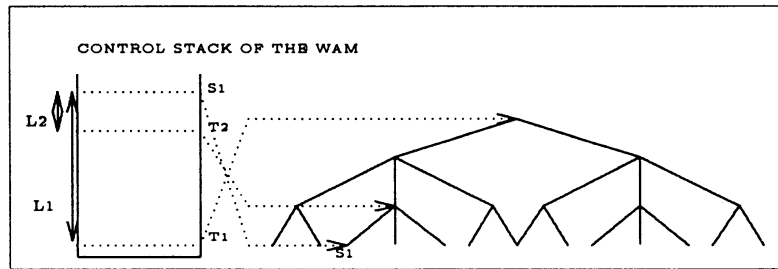


Figure 7: Granularity estimation of OR\_parallelism exploitation

close a worker is to reaching the next solution and therefore if it is worthwhile to share the work that leads to the next solution. PDP performs a granularity control for the exploitation of OR\_parallelism based on this observation. When a worker obtains a solution, it records the value of the backtracking stack top. The pending OR\_tasks are associated to a *choice point* in the backtracking stack. A pending OR\_task is sent to an idle worker only if the distance between the choice point and the top of the stack when the last solution was reached is greater than a critical value that is experimentally set. This test does not introduce run time overhead since only a comparison is needed. Figure 7 shows the stack size when solution  $S_1$  is reached. This point is very close to the choice point associated to the pending task  $T_2$  and therefore the distance  $L_2$  is smaller than the critical value  $C$ . This means, as the search tree shows, that  $T_2$  has a fine grain and therefore the task is kept in the worker. On the other hand, the task  $T_1$ , that corresponds to a choice point in the bottom of the stack, has a high granularity and is sent to an idle worker.

program	3 proc.		8 proc.		15 proc.	
	no c.	with c.	no c.	with c.	no c.	with c.
query	2.6	2.6	2.8	2.9	3.0	3.4
zebra	1.8	1.8	3.5	3.7	3.6	3.9
mm	2.1	2.1	3.2	3.4	4.1	4.5
queen(8)	2.9	2.8	7.0	7.3	12.3	12.9
queen(9)	2.4	2.4	7.5	7.7	13.8	14.2
queen(10)	3.0	3.1	7.8	7.9	14.5	14.7

Table 2: Speed-up achieved controlling OR\_parallelism granularity

Measurements have been taken to investigate the critical value  $C$ . On a system with 8 and 15 workers, this value, that depends on the system size is about  $stack\_size/6$ , where  $stack\_size$  is the size of the backtracking stack

when the last solution was reached. The speedup achieved by performing this procedure is shown in Table 2. For 3 workers the granularity control has no effect. For 8 workers the speedup increases for programs with a lot of parallel work (queen10). The greatest effect of the control is achieved on the system with 15 workers.

## 6 Performance Results

Our current implementation has been made in Parallel ANSI C on a Supernode (Parsys) with 16 T800 transputers connected in a torus network. In each processor the computation and communication functions have been split. There are three processes controlling the input, output and computation respectively.

The system does not support *cut* and database predicates yet, so the programs used to evaluate the system does not present these predicates. Some sequential programs have been tried in order to evaluate the overhead due to the parallel mechanism. The experiments demonstrate that the overhead when sequential programs are run on PDP is less than 5%. Results show that the overhead due to the writing down of the success path is less than 5%.

program	3 workers		8 workers		15 workers	
	copying	recomp.	copying	recomp.	copying	recomp.
query	2.8	2.6	3.0	2.9	3.4	3.4
zebra	1.9	1.8	3.6	3.7	3.1	3.9
mm	2.2	2.1	3.4	3.4	4.5	4.5
queen(8)	3.1	2.8	7.4	7.3	12.9	12.9
queen(9)	2.4	2.4	7.7	7.7	14.1	14.2
queen(10)	3.0	3.1	8.0	7.9	14.0	14.7

Table 3: OR\_parallelism speed-up with copying and recomputation approaches

We have compared speedup obtained exploiting OR\_parallelism using stack copying and recomputation approaches. All benchmarks have been executed in a "program, fail" way. The results obtained are shown in table 3. These results show significant speedup for all tested programs. Though the achieved speedup using stack copying and recomputation is quite similar, it is slightly greater with the copying approach using a smaller number of workers, and for programs with smaller granularity. On the other hand, it becomes greater with the recomputation approach when the system size increases. The reason for this is the smaller amount of information exchange in the recomputation approach. For queen10 the copying approach is more efficient

on a 3 or 8-worker system, while on a 15-worker system more efficiency is gained using the recomputation approach.

program	3 workers	8 workers	15 workers
qsort(700)	2.3	2.8	3.4
merge(500)	2.3	2.5	2.7

Table 4: AND\_parallelism speed-up

The exploitation of AND\_parallelism in PDP requires high granularity programs, since the workers sharing a job, exchange more messages than in the case of OR\_parallelism. Table 4 shows the speedup for *mergesort* and *qsortsort* programs, standard benchmarks used for AND\_parallel systems. For programs with more fine grain parallelism no speedup is achieved by exploiting AND\_parallelism.

In order to evaluate the behavior of PDP for programs with both kinds of parallelism, synthetic benchmarks with coarse grain parallelism have been run. The first one (synthetic 1) presents AND\_under\_OR parallelism:

```
:- check.
check :- times1(X),(p(X) & p(X) & p(X)).
check :- times2(X),(p(X) & p(X) & p(X)).
check :- times3(X),(p(X) & p(X) & p(X)).
times1(2000). times2(1000). times3(500).
p(0).
p(X) :- X > 0, X1 is X - 1, p(X1).
```

There is OR\_parallelism in the procedure *check* while AND\_parallelism appears in the body clauses of this procedure. The following benchmark (synthetic 2) presents OR\_under\_AND parallelism:

```
:- check(X).
check([Xs,Ys,Zs]) :- times(X), times(Y), times(Z), (p(X,Xs) & p(Y,Ys) & p(Z,Zs)).
p(X,Xs) :- p1(X,Xs).
p(X,Xs) :- p2(X,Xs).
p1(0,a).
p1(X,Xs) :- X > 0, X1 is X-1, p1(X1,Xs).
p2(0,b).
p2(X,Xs) :- X > 0, X1 is X-1, p2(X1,Xs).
times(1000).
```

There is AND\_parallelism in the body of the *check* clause, while the procedure *p* presents OR\_parallelism. Table 5 presents the speedup achieved by exploiting each kind of parallelism with 15 workers. Results show signifi-

program	OR_par.	AND_par.	Comb. par.
synthetic 1	1.5	2.9	4.5
synthetic 2	2.4	1.7	4.4

Table 5: OR, AND and Combining parallelism speed-up

cant speedup for all executions exploiting parallelism. The benchmark 1 has been chosen to show the advantages of exploring at the same time different solutions since the first solution explored by the sequential machine can be the slower to reach (the second clause of *check* is computed in a shorter time that the first one). It may be observed from the table that when both kinds of parallelism are exploited, the performance has been improved in all cases. The speedup achieved when exploiting both kinds of parallelism is greater than the product of the speedups achieved by exploiting each kind of parallelism separately. The reason is that the exploration of the different solutions when AND\_parallelism is exploited requires a number of messages exchanges between the parent worker and the worker exploring each goal in the parallel call (new solution requests and answers) that are avoided when OR\_under\_AND parallelism is exploited.

## 7 Conclusions

A system, PDP, to execute Prolog programs on distributed memory systems exploiting both, Independent\_AND and OR\_parallelism, has been presented. The execution model is based on multisequential Prolog engines that work independently under a hierarchic control. PDP deals with OR\_under\_AND parallelism producing in a distributed way the cross product of the solutions of the goals in a parallel call and creating a new computation for each combination. This avoids both the storage of partial solutions and the synchronization of workers. Results show that the overhead introduced to sequential execution is quite small. The overhead due to the exploitation mechanism of each kind of parallelism is also small. Different scheduling policies have been tested. The best result have been achieved when the nearest idle worker was chosen. This strategy is expected to yield even better results when the system size increases. Granularity controls have been introduced, showing a performance improvement when the system size increases. Significant speedup is achieved for coarse grain benchmark programs with each kind of parallelism. For some programs presenting both kinds of parallelism PDP achieves better results than the product of both. In the future the system will be extended to a larger number of workers and real applications will be tried.

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